

Quick poll $\int_2^k x^2 dx = 0$

↑
function of k

$$\left. \frac{x^3}{3} \right|_2^k = 0$$

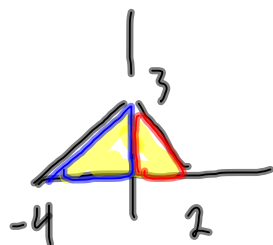
$$k = 2$$

$$3 \left(\frac{k^3}{3} - \frac{2^3}{3} = 0 \right)$$

$$k^3 = 8$$

Nov 19-9:10 AM

15



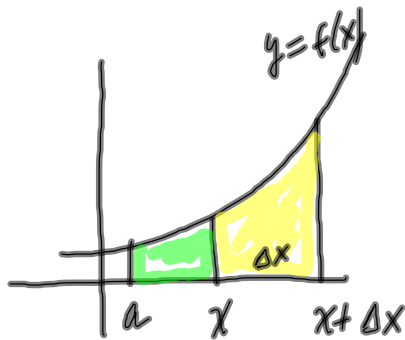
$$\bar{y} = \frac{1}{2 - (-4)} \int_{-4}^2 f(x) dx$$

area

$$\bar{y} = \frac{1}{6} \left(\frac{1}{2} \cdot \underline{6} \cdot 3 \right) = \frac{9}{6} = \frac{3}{2}$$

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5.4 Proof & use of the FTC

shaded area = ΔF

we noticed:

$$\lim_{\Delta x \rightarrow 0} \frac{\Delta F}{\Delta x} = f(x)$$

$$\lim_{\Delta x \rightarrow 0} \frac{F(x+\Delta x) - F(x)}{\Delta x} = f(x)$$

$$F'(x) = f(x)$$

FTC

says F is an antiderivative of f

$F(x)$ area function
(area from a to x)
 $\Delta F = F(x+\Delta x) - F(x)$

Nov 19-9:37 AM

restate FTC

version
I

$$\frac{d}{dx} \int_a^x f(t) dt = f(x)$$

$$\frac{d}{dx} F(x) = f(x)$$

$$F'(x) = f(x)$$

version
II

$$\int_a^b f(x) dx = F(b) - F(a)$$

where $F(x)$ is an antiderivative
of $f(x)$

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$$\frac{d}{dx} \int_{-\pi}^x \cos t \, dt = \cos x$$

\uparrow
 $f(t)$

$$\frac{d}{dx} \int_0^x \frac{1}{1+t^2} \, dt = \frac{1}{1+x^2}$$

Nov 19-10:08 AM

$$37. \int_{\pi/4}^{3\pi/4} \csc x \cot x \, dx = -\csc x \Big|_{\pi/4}^{3\pi/4}$$

use version II

$$= -\frac{1}{\sin \frac{3\pi}{4}} + \frac{1}{\sin \frac{\pi}{4}}$$

$$= -\frac{1}{\sqrt{2}/2} + \frac{1}{\sqrt{2}/2}$$

$$= 0$$

Nov 19-10:12 AM

44 find the total area bounded by
 $y = x^3 - 4x$ and the x -axis on
 $[-2, 2]$

$$\int_{-2}^2 x^3 - 4x \, dx = \left. \frac{x^4}{4} - 2x^2 \right|_{-2}^2 = \left(\frac{2^4}{4} - 2 \cdot 2^2 \right) - \left(\frac{(-2)^4}{4} - 2(-2)^2 \right) = 0$$

Nov 19-10:18 AM